## Year 1/AS Pure Mathematics PLC

1) ALGEBRAIC EXPRESSIONS

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :---: | :---: | :---: |
| Multiply and divide integer powers |  |  |  |
| Expand a single term over brackets and collect like terms |  |  |  |
| Expand the product of two or three expressions |  |  |  |
| Factorise linear, quadratic and simple cubic expressions |  |  |  |
| Know and use the laws of indices |  |  |  |
| Simplify and use the rules of surds |  |  |  |
| Rationalise denominators |  |  |  |

## 2) QUADRATICS

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Solve quadratic equations using factorisation, the quadratic formula <br> and completing the square |  |  |  |
| Read and use $\mathrm{f}(\mathrm{x})$ notation when working with functions |  |  |  |
| Sketch the graph and find the turning point of a quadratic function |  |  |  |
| Find and interpret the discriminant of a quadratic expression |  |  |  |
| Use and apply models that involve quadratic functions |  |  |  |

## 3) EQUATIONS AND INEQUALITIES

## I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Solve linear simultaneous equations using elimination or substitution |  |  |  |
| Solve simultaneous equations, one linear and one quadratic |  |  |  |
| Interpret algebraic solutions of equations graphically |  |  |  |
| Solve linear inequalities |  |  |  |
| Solve quadratic inequalities |  |  |  |
| Interpret inequalities graphically |  |  |  |
| Represent linear and quadratic inequalities graphically |  |  |  |

## 4) GRAPHS AND TRANSFORMATIONS

## I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :---: | :---: | :---: |
| Sketch cubic graphs |  |  |  |
| Sketch quadratic graphs |  |  |  |
| Sketch reciprocal graphs of the form $\mathrm{y}=\mathrm{a} / \mathrm{x}$ and $\mathrm{y}=\mathrm{a} / \mathrm{x}^{2}$ |  |  |  |
| Use intersection points of graphs to solve equations |  |  |  |
| Translate graphs |  |  |  |
| Stretch graphs |  |  |  |
| Transform graphs of unfamiliar functions |  |  |  |

## 5) STRAIGHT LINE GRAPHS

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Calculate the gradient of a line joining a pair of points |  |  |  |
| Understand the link between the equation of a line, its gradient and <br> intercept |  |  |  |
| Find the equation of a line given (i) the gradient and one point on the <br> line or (ii) two points on the line |  |  |  |
| Find the point of intersection for a pair of straight lines |  |  |  |
| Know and use the rules for parallel and perpendicular gradients(lines) |  |  |  |
| Solve length and area problems on coordinate grids |  |  |  |
| Use straight line graphs to construct mathematical models |  |  |  |

## 6) CIRCLES

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :---: | :---: | :---: |
| Find the midpoint of a line segment |  |  |  |
| Find the equation of the perpendicular bisector to a line segment |  |  |  |
| Know how to find the equation of a circle |  |  |  |
| Solve geometric problems involving straight lines and circles |  |  |  |
| Use circle properties to solve problems on coordinate grids |  |  |  |
| Find the angle in a semicircle and solve other problems involving <br> circles and triangles |  |  |  |

## 7) ALGEBRAIC METHODS

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :---: | :---: | :---: |
| Cancel factors in algebraic fractions |  |  |  |
| Divide a polynomial by a linear expression |  |  |  |
| Use the factor theorem to factorise a cubic expression |  |  |  |
| Construct mathematical proofs using algebra |  |  |  |
| Use proof by exhaustion and disproof by counter-example |  |  |  |

## 8) THE BINOMIAL EXPANSION

## I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Use Pascal's Triangle to identify binomial coefficients and use them to <br> expand simple binomial expansions |  |  |  |
| Use combinations and factorial notations |  |  |  |
| Use the binomial expansion to expand brackets |  |  |  |
| Find individual coefficients in a binomial expansion |  |  |  |
| Make approximations using the binomial expansion |  |  |  |

## 9) TRIGONOMETRIC RATIOS

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :---: | :---: | :---: |
| Use the Cosine rule to find a missing side or angle |  |  |  |
| Use the Sine rule to find a missing side or angle |  |  |  |
| Find the area of a triangle using an appropriate formula |  |  |  |
| Solve problems involving triangles |  |  |  |
| Sketch the graphs of the sine, cosine and tangent functions |  |  |  |
| Sketch simple transformations of sine, cosine and tangent graphs |  |  |  |
|  |  |  |  |

## 10) TRIGONOMETRIC IDENTITIES AND EQUATIONS

I am able to...

|  | (-) | $\because$ | ¢) |
| :---: | :---: | :---: | :---: |
| Calculate the sine, cosine and tangent of any angle |  |  |  |
| Know and use the exact trigonometric ratios for 30, 45 and 60 |  |  |  |
| Know and use the relationships $\tan \theta=\sin \theta / \cos \theta$ and $\cos ^{2} \theta+\operatorname{Sin}^{2} \theta=1$ |  |  |  |
| Solve simple trigonometric equations of the forms $\sin \theta=k, \cos \theta=k$ and $\tan \Theta=k$ |  |  |  |
| Solve more challenging trigonometric equations of the forms $\sin n \theta=k$ and $\sin (n \Theta \pm \mu)=k$ and equivalent equations involving $\cos$ and $\tan$ |  |  |  |
| Solve trigonometric equations that produce quadratics |  |  |  |

## 11) VECTORS

## I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Use vectors in two dimensions |  |  |  |
| Use column vectors and carry out arithmetic operations on vectors |  |  |  |
| Calculate the magnitude and direction of a vector |  |  |  |
| Understand and use position vectors |  |  |  |
| Use vectors to solve geometric problems |  |  |  |
| Understand vector magnitude and use vectors in speed and distance <br> calculations |  |  |  |
| Use vectors to solve problems in context |  |  |  |
|  |  |  |  |

## 12) DIFFERENTIATION

I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Find the derivative, $\mathrm{f}^{\prime}(\mathrm{x})$ or $\mathrm{dy} / \mathrm{dx}$, of a simple function |  |  |  |
| Use the derivative to solve problems involving gradients, tangents and <br> normals |  |  |  |
| Identify increasing and decreasing functions |  |  |  |
| Find the second order derivative, $\mathrm{f}^{\prime \prime}(\mathrm{x})$ or $\mathrm{d}^{2} \mathrm{y} / \mathrm{dx}^{2}$ of a simple function |  |  |  |
| Find stationary points of functions and determine their nature |  |  |  |
| Sketch the gradient function of a given function |  |  |  |
| Model real-life situations with differentiation |  |  |  |

## 13) INTEGRATIATION

## I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :---: | :---: | :---: |
| Find $y$ given $d y / d x$ or $x^{n}$ |  |  |  |
| Integrate polynomials |  |  |  |
| Find $f(x)$ given $\mathrm{f}^{\prime}(\mathrm{x})$ and a point on the curve |  |  |  |
| Evaluate a definite integral |  |  |  |
| Find the area bounded by a curve and the x -axis |  |  |  |
| Find areas bounded by curves and straight lines |  |  |  |
|  |  |  |  |

## 14) EXPONENTIALS AND LOGARITHMS

## I am able to...

|  | $\ddots$ | $\ddots$ | $\ddots$ |
| :--- | :--- | :--- | :--- |
| Sketch graphs of the form $\mathrm{y}=\mathrm{a}^{\mathrm{x}}, \mathrm{y}=\mathrm{e}^{\mathrm{x}}$ and transformations of these <br> graphs |  |  |  |
| Differentiate $\mathrm{e}^{\mathrm{kx}}$ and understand why this result is important |  |  |  |
| Use and interpret models that use exponential functions |  |  |  |
| Recognise the relationship between exponents and logarithms |  |  |  |
| Recall and apply the laws of logarithms |  |  |  |
| Solve equations of the form $\mathrm{a}^{\mathrm{x}}=\mathrm{b}$ |  |  |  |
| Describe and use the natural logarithm function |  |  |  |
| Use logarithms to estimate the values of constants in non-linear models |  |  |  |

